Time Reversal Using the FDTD Method – Allison Tanner

$_{tz}$ Formulation for 1D TEz

$$H_z^{n-\frac{1}{2}}(i) = C_{hzey}\left(E_y^n(i+1) - E_y^n(i)\right) - C_{hzh}H_z^{n+\frac{1}{2}}(i) \tag{1a}$$

Where...

$$C_{hzey} = \frac{-2\Delta t}{(\Delta x)(\Delta t \sigma_x^m(i) - 2\mu_z(i))}, \quad C_{hzh} = \left(\frac{\Delta t \sigma_x^m(i) + 2\mu_z(i)}{\Delta t \sigma_x^m(i) - 2\mu_z(i)}\right)$$
 [1b]

Ey

$$E_y^n(i) = C_{eyhz} \left(H_y^{n + \frac{1}{2}}(i) - H_y^{n + \frac{1}{2}}(i - 1) \right) - C_{eye} \left(E_z^{n+1}(i) \right)$$
 [2a]

$$C_{eyhz} = \frac{-2\Delta t}{\Delta x (\Delta t \sigma_y^e - 2\varepsilon_y)}, \quad C_{eye} = \left(\frac{\Delta t \sigma_y^e + 2\varepsilon_y}{\Delta t \sigma_y^e - 2\varepsilon_y}\right)$$
 [2b]

Formulation for 2D TEz

$$E_x^n(i,j) = C_{exhz}(i,j) \left(H_z^{n+\frac{1}{2}}(i,j) - H_z^{n+\frac{1}{2}}(i,j-1) \right) - C_{exe}(i,j) E_x^{n+1}(i,j)$$
 [1a]

$$C_{exe}(i,j) = \begin{pmatrix} \frac{\Delta t \sigma_X^{\theta}(i,j) + 2\varepsilon_X(i,j)}{\Delta t \sigma_X^{\theta}(i,j) - 2\varepsilon_X(i,j)} \end{pmatrix} \qquad C_{exhz}(i,j) = \frac{2\Delta t}{\Delta y \left(\Delta t \sigma_X^{\theta}(i,j) - 2\varepsilon_X(i,j)\right)}$$
 [1b]

$$E_{y}^{n}(i,j) = -C_{eyhz}(i,j) \left(H_{z}^{n+\frac{1}{2}}(i,j) - H_{z}^{n+\frac{1}{2}}(i-1,j) \right) - C_{eye}(i,j) E_{y}^{n+1}(i,j)$$
 [2a]

$$C_{eye}(i,j) = \left(\frac{\Delta t \sigma_y^{\varrho}(i,j) + 2\varepsilon_y(i,j)}{\Delta t \sigma_y^{\varrho}(i,j) - 2\varepsilon_y(i,j)}\right) \qquad \qquad C_{eyhz}(i,j) = \frac{2\Delta t}{\Delta x \left(\Delta t \sigma_y^{\varrho}(i,j) - 2\varepsilon_y(i,j)\right)}$$
 [2b]

$$H_z^{n-\frac{1}{2}}(i,j) = C_{hzex}(i,j) \left(E_x^n(i,j+1) - E_x^n(i,j) \right) - C_{hzey}(i,j) \left(E_y^n(i+1,j) - E_y^n(i,j) \right) - C_{hzey}(i,j) H_z^{n+\frac{1}{2}}(i,j)$$
[3a]

$$C_{hzex}\left(i,j\right) = \frac{2\Delta t}{\Delta y \left(\Delta t \sigma_z^m(i,j) - 2\mu_z(i,j)\right)}, C_{hzey}\left(i,j\right) = \frac{2\Delta t}{\Delta x \left(\Delta t \sigma_z^m(i,j) - 2\mu_z(i,j)\right)}, C_{hzh}\left(i,j\right) = \left(\frac{\Delta t \sigma_z^m(i,j) + 2\mu_z(i,j)}{\Delta t \sigma_z^m(i,j) - 2\mu_z(i,j)}\right)$$
[3b]

Simulation of 1D Time Reversal with FDTD in Matlab







